

**Geophysics 424 A1      Final exam**  
**Electromagnetic and Potential field methods**

**Date :**                    Wednesday December 9<sup>th</sup> 2009, 2pm – 5pm  
**Location**                CEB 4-42  
**Instructor :**          Dr. Martyn Unsworth  
**Time allowed :** 3 hours  
**Total points = 100**

**Instructions**

*Attempt all questions.*

*Notes and books may **not** be used.*

*Calculators may be used.*

*Cell phones and all other electronic devices must be switched off and stored.*

*All questions must be directed to the invigilator.*

*A separate 2 page formula sheet is available.*

**Question 1 : Resistivity of rocks (Total = 11 points)**

(a) Electric current flows in a material that contains a single type of charge carrier.

There are  $n$  charge carriers per unit volume and each has a charge  $q$ .

The charge carriers have a mobility  $\mu$  which is defined as the drift velocity per unit electric field.  $\mu = \frac{\bar{v}}{E}$

Show that the electrical conductivity of the material is given by  $\sigma = n\mu q$

**(6 points)**

(b) A brine is formed by dissolving 30 g of sodium chloride in 1 liter of water.

The brine has a conductivity of 3 S/m.

Estimate the mobility of the ions. You can assume that the sodium ( $\text{Na}^+$ ) and chloride ( $\text{Cl}^-$ ) ions have the same mobility

**(5 points)**

**Useful data**

Volume of 1 liter of water	$10^{-3} \text{ m}^3$
Molar weight of sodium chloride	58.4 g / mol
Avogadro's number	$6.02 \cdot 10^{23}$
Charge on electron	$1.6 \cdot 10^{-19} \text{ C}$

**Question 2 : Marine EM methods (Total = 14 points)**

- How does frequency domain marine controlled source EM exploration measure variations of resistivity with depth?
- In a study area, the seafloor has a uniform porosity of 10% and the pore space is poorly connected. The seawater conductivity is 3 S/m. It is required to transmit EM signals over a distance of 5 km through the seafloor. What transmission frequency is needed?
- Explain the difference of **broadside** and **inline** configurations. How are they used to detect **hydrocarbon reservoirs**? Include a diagram in your answer.

**Question 3 : Frequency domain EM (Total = 26 points)**

- (a) A **good conductor** generates a secondary magnetic field that is **in-phase** with the primary magnetic field. Explain the **physics** of this observation in detail.

Your answer should include a **phase diagram**.

**(6 points)**

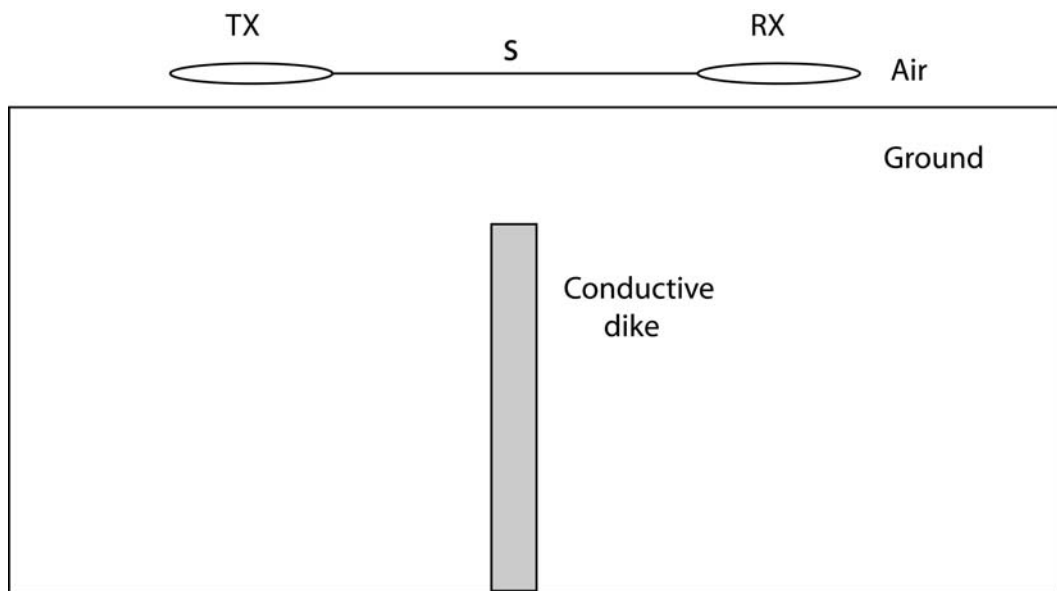
- (b) An EM survey uses **horizontal co-planar** transmitter and receiver loops.

Consider the situation when the transmitter (TX) and receiver (RX) are located above a conductive dike.

Sketch the primary magnetic field ( $H^P$ ) and **in-phase** secondary magnetic field ( $H^S$ ) lines on the diagram below.

What will be the **sign** of  $\frac{H^S}{H^P}$  at the receiver?

**(6 points)**



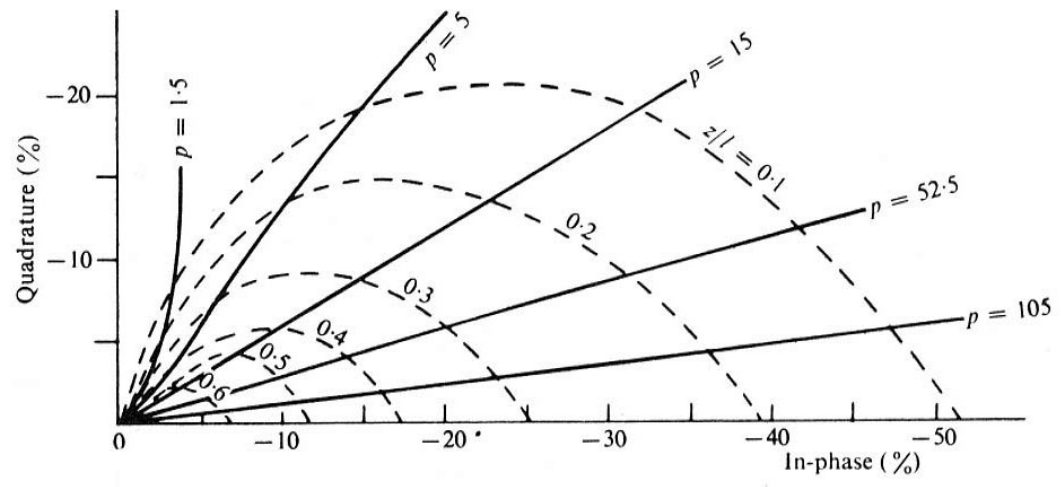
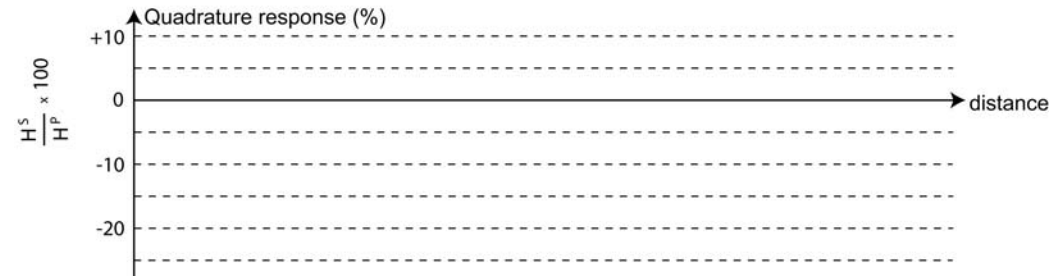
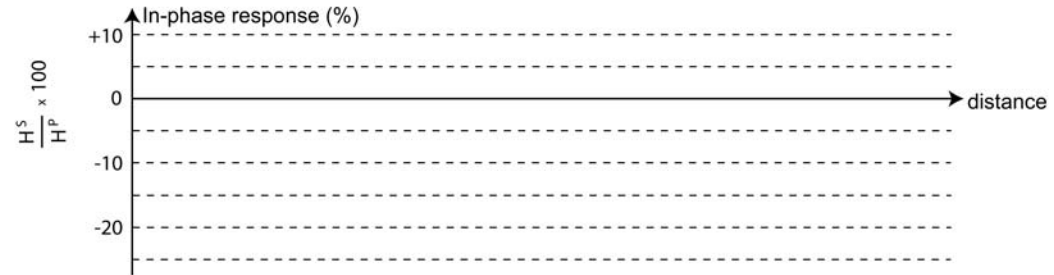
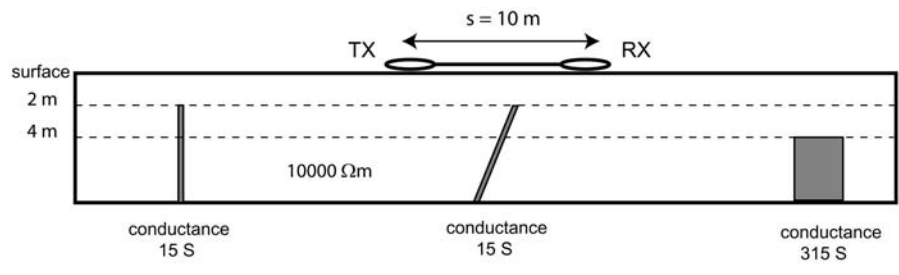
- (c) The figure on the next page shows three basement conductors. Sketch the **in-phase** and **quadrature** responses along the profile that would be obtained with an EM system using a frequency of 4200 Hz

Use the **characteristic curves** to be **quantitative** where possible.

Response parameter,  $p = \mu\omega\sigma Ws$  (constant on solid lines)  
 Depth parameter,  $D = z / s$  (constant on dashed lines)

$W$  = width of conductor  
 $\sigma$  = conductivity of conductor  
 $z$  = depth to conductor

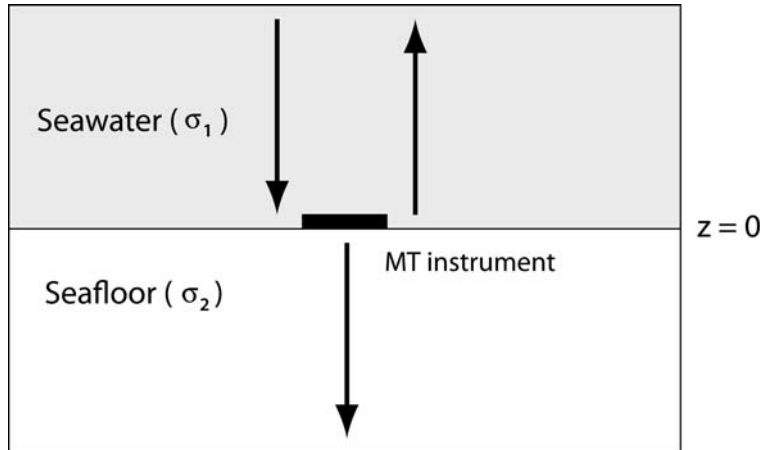
$s$  = TX-RX separation,  
 $\omega$  = TX frequency (rad /s)



(14 points)

**Question 4 : Maxwell's Equations (Total = 21 points)**

A seafloor MT survey is being used to measure the resistivity of the seafloor. A **plane** EM wave has an angular frequency,  $\omega$ , and travels **vertically** downwards in seawater in the  $z$ -direction. The electric field is **polarized** in the  $x$ -direction.



Down going signal in seawater

$$E_x(z,t) = Ae^{-k_1z} e^{-i\omega t}$$

Up going signal in seawater

$$E_x(z,t) = Be^{k_1z} e^{-i\omega t}$$

Down going signal in seafloor

$$E_x(z,t) = Ce^{-k_2z} e^{-i\omega t}$$

$$k_1 = \sqrt{-i\omega\mu_0\sigma_1} \text{ and } k_2 = \sqrt{-i\omega\mu_0\sigma_2}$$

(a) Use Maxwell's equations to prove that the **horizontal electric** field is continuous at the seafloor ( $z = 0$ )

**(5 points)**

(b) Use Maxwell's equations to show that for this plane, polarized EM signal

$$H_y(z) = \frac{1}{i\omega\mu} \frac{\partial E_x(z)}{\partial z} \quad \text{(5 points)}$$

(c) Derive an expression for  $\frac{C}{A}$  at the seafloor in terms of  $\sigma_1$  and  $\sigma_2$ . State any boundary conditions that you use.

**(6 points)**

(d) The MT instrument measures electric and magnetic fields at a frequency  $\omega$ .

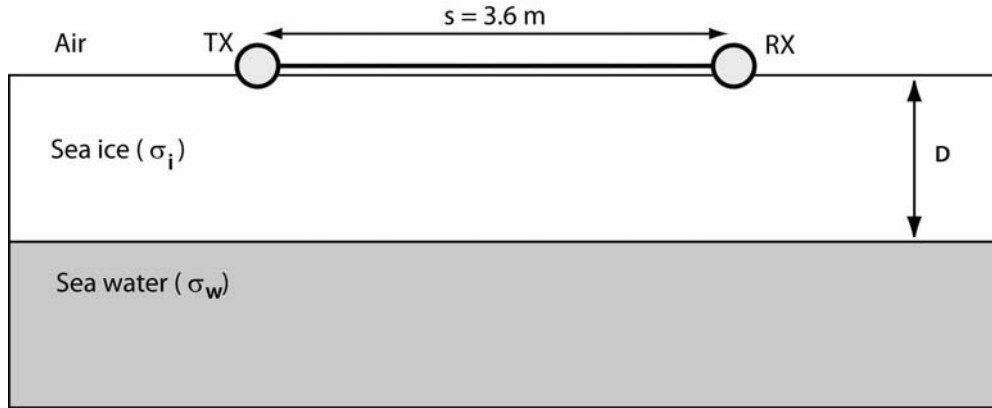
At  $z = 0$ , the measured electric and magnetic fields is  $E_x^m$  and  $H_y^m$

Derive an equation for the seafloor conductivity ( $\sigma_2$ ) in terms of  $E_x^m$  and  $H_y^m$

**(5 points)**

**Question 5 : Frequency domain EM methods (Total = 17 points)**

An EM31 survey is being used to measure sea-ice thickness with a frequency of 9100 Hz. The transmitter and receiver dipoles are oriented **horizontally** and placed on the ice. The sea-ice has a conductivity  $\sigma_i$  and the seawater has a conductivity  $\sigma_w$ .

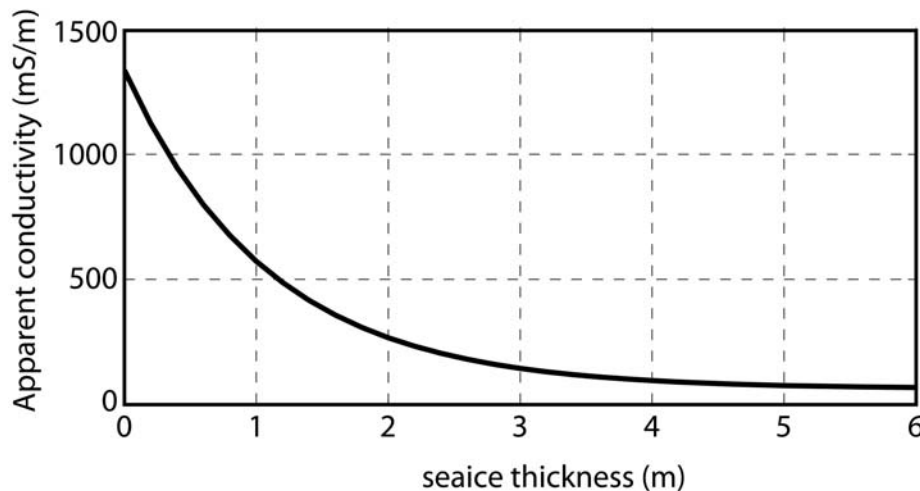


(a) Write down an equation for the **average conductivity**  $\bar{\sigma}_h$  measured by the EM31. **(3 points)**

(b) Studies have shown that  $\sigma_i = 23 \text{ mS/m}$  and  $\sigma_w = 2600 \text{ mS/m}$

Compute  $\bar{\sigma}_h$  for  $D = 2, 3$  and  $4 \text{ m}$ . Plot your results on the graph below.

**(7 points)**



(c) The instrument reading was 600 mS/m. Estimate the ice thickness (D) at this location from the graph you plotted in (b) **(2 points)**

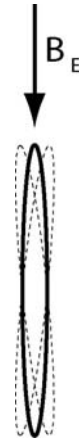
(d) The black line on the figure shows the results of a calibration test where the ice thickness was measured by coring. Compare your answer to that from (b) and suggest an explanation for any differences. **(5 points)**

**Question 6 : Time domain EM methods (Total = 11 points)**

- (a) A time domain EM survey is being conducted at a location where the Earth's magnetic field is **vertical** and  $B_E = 50000$  nT.

The x-axis receiver coil oscillates with an amplitude of  $1^\circ$  at a frequency of 0.5 Hz.

What noise level does this produce in  $\frac{dB_z}{dt}$  ?



**(4 points)**

- (b) The transmitter has a current  $I = 100$  amps, area  $A = 100 \text{ m}^2$  and 5 turns of wire ( $N = 5$ ).

The noise level is that computed in part (a)

The Earth has a resistivity of  $200 \text{ } \Omega\text{m}$

What is the **latest time** at which the transient can be observed? **(4 points)**

What is **maximum depth of exploration** at this location? **(3 points)**