4.9 – Antiderivatives

Def'n: A function F(x) is an <u>antiderivative</u> of f(x) if F'(x) = f(x).

Ex4.10) Find three antiderivatives of $f(x) = \cos(2x)$.

Remark: The general antiderivative of f(x) is F(x) + c, where c is a constant.

Ex4.11) Find the general antiderivative of $f(x) = \sec^2 x$.

Ex4.12) Find the antiderivative of $f(x) = \frac{1}{2\sqrt{x}}$ that satisfies F(4) = 0.

Remark: There are many nice rules for differentiation: constant multiple, product, power, quotient, chain, etc. There are not so many nice rules for antidifferentiation. But...

Antidifferentiation Rules:

- 1. Constant Multiple:
- 2. Sum/Difference:
- 3. Power Rule:

Ex4.13) Find the general antiderivatives of:

1.
$$f(x) = 6x$$

2.
$$f(x) = x^7$$

3.
$$f(x) = x^7 - 6x + 8$$

4.
$$f(x) = \frac{2}{x^3}$$

5.
$$f(x) = \frac{4}{3}\sqrt[3]{x}$$

6.
$$f(x) = \frac{1}{2\sqrt{x}}$$

7.
$$f(x) = \pi \cos(\pi x)$$

8.
$$f(x) = \csc x \cot x$$

9.
$$f(x) = 34e^x$$

10.
$$f(x) = \frac{x^2 - x^{\frac{3}{2}}}{\sqrt{x}}$$

11. A rocket lifts off from Earth at an acceleration of 20m/s². How fast will the rocket be going 1 minute later?

Def'n: The set of all antiderivatives of a function f(x) is called the indefinite integral of f. It is denoted $\int f(x)dx$

 \int is an <u>integral sign</u>. The function f(x) is called the <u>integrand</u>.

Ex4.14)

$$1. \int (3x+2)dx$$

2.
$$\int (32x^5 - 18x^3) dx$$

$$3. \int \left(\frac{2}{x^3} - \frac{7}{4}\sqrt[3]{x^5}\right) dx$$

$$4. \int \cos x \, dx$$

$$5. \int \left(3e^x - \frac{3}{x}\right) dx$$

Practice: 4.9 ODDS