

2.8 The Derivative as a Function

Notation: Given a function $f(x)$, the derivative of $f(x)$ is also a function, which is notated

$$f'(x) \text{ or } \frac{df}{dx} \text{ or } \frac{d}{dx}f(x)$$

Ex2.29) Calculate $f'(x)$ when $f(x) = \frac{1}{2+x}$.

Def'n: A function is differentiable at a point a if its derivative exists there. That is, $f(x)$ must be continuous at a and "smooth" at a .

Three situations make $f(x)$ non-differentiable at a point a .

1. A "corner".
2. A discontinuity.
3. A vertical tangent.

Ex2.30) What values of m and b make f differentiable everywhere?

$$f(x) = \begin{cases} x^2 & , \quad x \leq 2 \\ mx + b & , \quad x > 2 \end{cases}$$

Notice that $f'(x) > 0$ whenever $f(x)$ is rising to the right and $f'(x) < 0$ whenever $f(x)$ is falling to the right.