

Demo_3_Lapis_2019_Steepest_Descent

April 8, 2019

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In [1]: using PyPlot, LinearAlgebra, Random
```

```
In [7]: # Make a matrix...
```

```
Random.seed!(1234)
A=randn(5,2).^3
U,S,V=svd(A)
S=[1,0.4]
A=U*diagm(0 =>S)*V'
```

0.1 Steepest descent method with Matrices (Operators)

```
In [5]: x0 = [0.0,2.0]
        y = A*x0
```

```
N,M = size(A)
```

```
x1 = collect(-8:0.1:8)
x2 = collect(-8:0.1:8)
J = zeros(length(x2),length(x1))
for i = 1:length(x1)
    for j=1:length(x2)
        J[j,i] = sum((A*[x1[i],x2[j]]-y).^2)
    end
end
```

```
K = 50
v1 = zeros(K)
v2 = zeros(K)
x = [-6,-7]
```

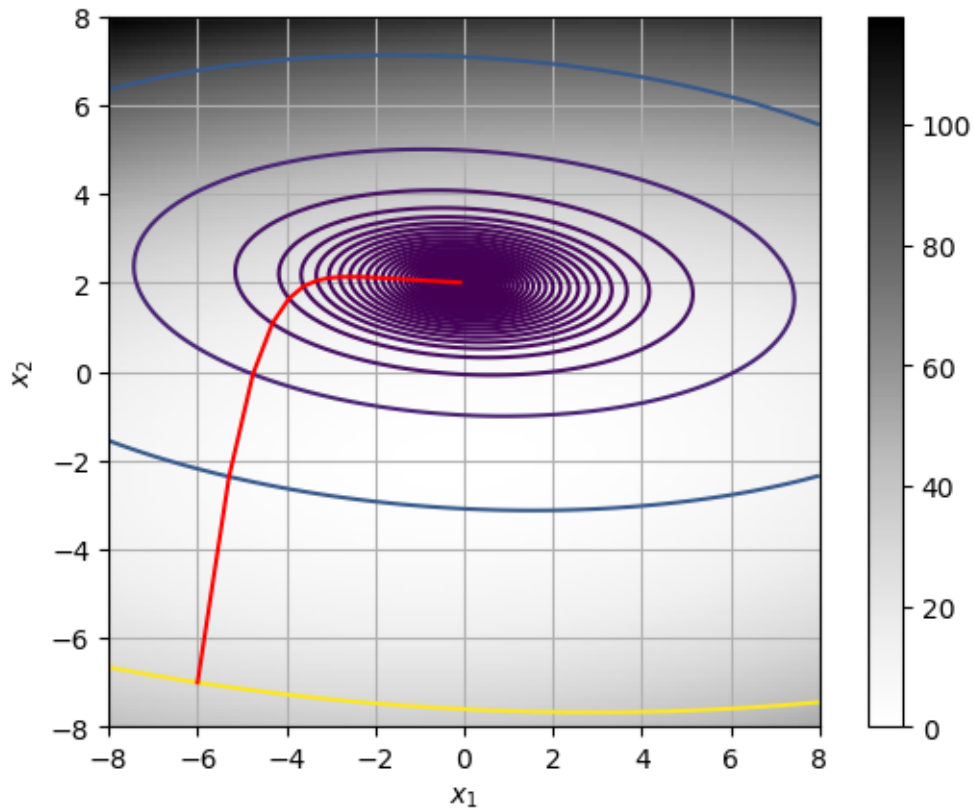
```
v1[1] = x[1];
v2[1] = x[2];
cc= zeros(K)
cc[1] = sum((A*x-y).^2)
for k = 1:K-1
```

```

e = A*x-y
g = A'*e
alpha=0.5
x = x - alpha*g
v1[k+1]=x[1]
v2[k+1]=x[2]
cc[k+1] = sum((A*x-y).^2)
end

contour(x1,x2,J,sort(cc))
imshow(J, extent=(-8,8,-8,8), cmap="Greys")
colorbar()
plot(v1,v2,"r")
xlabel(L"$x_1$")
ylabel(L"$x_2$")
grid(true);

```



In [6]: x

```

Out[6]: 2-element Array{Float64,1}:
-0.09169476740058996
 2.005368985494076

```