# Faculty of Engineering and Department of Physics 

## Engineering Physics 131

Final Examination
Saturday April 21, 2018; 14:00 pm - 16:30 pm

1. Closed book exam. No notes or textbooks allowed.
2. Formula sheets are included (may be removed).
3. The exam has 9 problems and is out of $\mathbf{6 1 . 5}$ marks. Attempt all parts of all problems.
4. Questions 1 to 4 do not require detailed calculations and only the final answers to these questions will be marked.
5. For Questions 5 to 9, details and procedures to solve these problems will be marked. Show all work in a neat and logical manner.
6. Write your solution directly on the pages with the questions. Indicate clearly if you use the backs of pages for material to be marked.
7. Only non-programmable calculator approved by the Faculty of Engineering permitted. Turn off all cell-phones, laptops, etc.

DO NOT separate the pages of the exam containing the problems.

LAST NAME: $\qquad$

FIRST NAME:

ID\#:

Please circle the name of your instructor:

EB01: Wheelock EB02: Jung
EB03: Wang EB04: Kim

EB05: Gingrich EB06: Tang


#### Abstract

Address all inquiries to a supervisor. Do not communicate with other candidates. If you become ill during the exam, contact a supervisor immediately. (You may not claim extenuating circumstances and request your paper to be cancelled after writing and handing in your examination.) You may not leave the exam until at least 30 minutes have elapsed

End of Exam: When the signal is given to end the exam, students must promptly cease writing. If a student does not stop at the signal, the instructor has the discretion either not to grade the exam paper or to lower the grade on the examination.


## Exam Collection Procedure

-If you finish early, stay in your seat and raise your hand
-Someone will come to collect your exam (after which you may quietly leave)
-In the final 10 minutes: please remain seated until ALL exams have been collected.

Please do not write in the table below.

| Question | Value (marks) | Mark |
| :--- | :--- | :--- |
| 1 | 4.5 |  |
| 2 | 4 |  |
| 3 | 4 |  |
| 4 | 4 |  |
| 5 | 10 |  |
| 6 | 10 |  |
| 7 | 9 |  |
| 8 | 8 |  |
| 9 | 8 |  |
| Total | 61.5 |  |

## Q1. [4.5 marks]

A block weighing 22 N is held at rest against a vertical wall by a horizontal force $\boldsymbol{F}$ of magnitude 60 N . The coefficient of static friction between the wall and the block is 0.55 , and the coefficient of kinetic friction between them is 0.38 . A second force $\boldsymbol{P}$ is applied to the block and directed parallel to the wall with the magnitudes and directions shown in the figures and table below.

For each value of P in the table below, determine: the magnitude of the frictional force; whether the block moves up, down or remains stationary; and whether the frictional force (between block and wall) is directed downward. Write your answers in the table.
[0.5 marks for each answer, no partial marks]


| Force $\boldsymbol{P}$ <br> $(\mathrm{N})$ | Magnitude of <br> frictional force (N) | Block moves <br> (no/up/down) | Frictional force down <br> the wall (yes/no) |
| :---: | :---: | :---: | :---: |
| 12, up <br> (figure A) |  |  |  |
| 62, up <br> (figure A) |  |  |  |
| 10, down <br> (figure B) |  |  |  |

## Q2. [4 marks]

For each of the scenarios below, circle ALL the forces that could contribute to the normal acceleration $a_{n}$ of the specified particle. Please Note: "Friction" may be static or kinetic, "Normal force" is the support force on the specified particle from the surface it is in contact with.
[1 mark for each scenario, no partial marks, all correct answers must be selected in order to receive the 1 mark.]
(a) A rough bar rotates in the vertical plane about point $O$. Collar $A$ moves together with the bar without relative motion. Consider collar $A$ as the particle and it is at the position shown.

Normal force
Friction
Gravity

(b) Block $B$ is sliding down the rough circular track, which is in the vertical plane. Consider block $B$ as the particle and it is at the position shown.

Normal force
Friction
Gravity

(c) The rough circular bar rotates about the vertical axis $A B$. The mass $m$ remains stationary relative to the circular bar. Consider mass $m$ as the particle and it is at the position shown.

Normal force
Friction
Gravity

(d) A motorcycle (the particle considered here) moves along a circular track on a flat rough surface.

Normal force
Friction Gravity


## Q3. [4 marks]

A block is held at rest at location A against a massless spring that is initially compressed a distance x relative to its resting length $L$. When the spring is released, the block slides to the right, up a circular ramp, then exits the ramp vertically at D , and finally reaches its maximum elevation at location E . Assume that all surfaces are smooth except the rough portion of the ramp between B and C as shown in the diagram. Neglect air resistance.

As the block moves along each segment of its path, consider whether the work done by each force is positive, negative or zero. In the table below, circle the correct answer in each box.

No partial credit; for each row, all answers must be correct to receive credit.


| Segment | Gravitational <br> force | Friction | Spring force | Normal force |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| (a) [1 mark] <br> From A to B | + | 0 | - | + | 0 | - | + | 0 | - | + | 0 |$--$

(d) $[1$ mark $]$ Now consider the total work done by all forces acting on the block, as it moves from its initial position at A to location E. Is the total work positive, negative or zero? Circle the correct entry below.

| Segment | Total Work |  |
| :--- | :---: | :---: | :--- |
| From A to E | $+\quad 0$ | - |

## Q4. [4 marks]

At time $t=0$, a $5-\mathrm{kg}$ toy car moves in the $x-y$ plane at a velocity given by $\mathbf{v}=-5 \mathbf{i}+2 \mathbf{j} \mathrm{~m} / \mathrm{s}$. The graph gives the component $F_{x}$ of the total force acting on the toy car. The component $F_{y}$ is equal to zero.

Please include appropriate units. No partial marks. Only the final answers will be marked; detailed calculations are not required.

(a) [1 mark] What are the $x$ and $y$ components of the impulse on this toy car between $t=0$ and 6 s ?
$\qquad$
$I_{x}=$

$$
I_{y}=
$$

(b) [1 mark] What are the $x$ and $y$ components of the impulse on this toy car between $t=0$ and 9 s ?
$I_{x}=$ $\qquad$

$$
I_{y}=
$$

(c) [1 mark] What is the toy car's velocity at $t=6 \mathrm{~s}$ ? (Give the velocity's magnitude and angle measured from the positive $\mathbf{i}$ direction counterclockwise.)
magnitude: $\qquad$ angle: $\qquad$
(d) [1 mark] What is the toy car's velocity at $t=9 \mathrm{~s}$ ? (Give the velocity's magnitude and angle measured from the positive $\mathbf{i}$ direction counterclockwise.)
magnitude: $\qquad$ angle: $\qquad$

## Q5. [10 marks]

Consider the motion of a cart as shown. A uniform cylinder rests on the cart and remains stationary relative to the cart during the motion.
(a) [5 marks] Consider the figure on the left below. For a given horizontal force $\boldsymbol{P}$, determine the normal reaction forces at $A$ and $B$. The angle $\theta=60^{\circ}$. The mass of the cylinder is $m$ and that of the cart is $M$. Neglect all friction.
(b) [5 marks] The system is now placed on the $\phi=15^{\circ}$ incline as shown in the figure on the right below. What force $\boldsymbol{P}$ will cause the normal reaction force at $B$ to be zero?

Express your answers in terms of $\mathrm{P}, \mathrm{M}, \mathrm{m}$ and g (gravitational acceleration). Box your answer.


## Q6. [10 marks]

At the instant shown, the cable attached to the cart of mass $m_{1}=0.4 \mathrm{~kg}$ is tangent to the smooth circular path of the cart. The cylinder has mass $m_{2}=0.6 \mathrm{~kg}$ and the mass of the pulley is negligible. $R=1.75 \mathrm{~m}$ and $\beta=30^{\circ}$.
(a) [5 marks] Determine the acceleration of $m_{2}$ and the tension $T$ in the cable.
(b) [5 marks] At this instance what would be the maximum speed $v_{2}$ of $m_{2}$ for which $m_{1}$ remains in contact with the surface?

Box your answer.


## Q7. [9 marks]

A $50-\mathrm{kg}$ crate is initially at rest on an incline. Starting at $t=0$, the motor supplies a rope tension of $T$ $=10 t^{2} N$, where t is in seconds. The coefficients of static and kinetic friction between the crate and the incline are 0.6 and 0.4 respectively. You may assume that the pulleys are massless and frictionless.
(a) [3 marks] Find the time $t_{l}$ when the crate begins to move.
(b) [4 marks] What is the speed of the crate when $t=6 s$ ?
(c) [2 marks] If the power input to the motor is 6000 W when $t=6 s$, what is the efficiency at this instant?

Box your answer.


## Q8. [8 marks]

Two disks $\mathbf{A}$ and $\mathbf{B}$ each have weight of 2 lb and slide on a smooth horizontal surface (with no friction). They have initial speeds $\left(\mathrm{V}_{\mathrm{A}}\right)_{1}=4 \mathrm{ft} / \mathrm{s}$ and $\left(\mathrm{V}_{\mathrm{B}}\right)_{1}=3 \mathrm{ft} / \mathrm{s}$ just before they collide. The initial velocity vectors are shown in the figure below. If $\mathrm{e}=0.5$ determine their velocities (magnitudes and directions) just after impact.

Box your answer.


## Q9. [8 marks]

A uniform solid sphere, of mass 10 kg and radius 0.6 m , is initially held so that its centre of mass being at the same height as point $\mathbf{A}$, as shown by the dotted line in the figure $\left(\theta=0^{0}\right)$. The sphere is then released from rest, allowing it to rotate downward about the frictionless hinge at $\mathbf{A}$.
(a) [4 marks] Determine the angular velocity of the sphere when $\theta=60^{\circ}$.
(b) $[4$ marks $]$ Determine the angular acceleration of the sphere when $\theta=60^{\circ}$.

Box your answer.

## 10 kg



## Table of Moment of Inertia

(a) Slender rod,
axis through center
(b) Slender rod,
(c) Rectangular plate,
axis through center
(d) Thin rectangular plate, axis through one end
axis along edge

(e) Hollow cylinder

$$
I=\frac{1}{2} M\left(R_{1}^{2}+R_{2}^{2}\right)
$$

(f) Solid cylinder


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(g) Thin-walled hollow cylinder $I=M R^{2}$

(h) Solid sphere

(i) Thin-walled hollow


Fundamental Equations of Dynamics


| Equations of Motion |
| :--- | :--- |
| Particle $\Sigma \mathbf{F}=m \mathbf{a}$ <br> Rigid Body $\Sigma F_{x}=m\left(a_{G}\right)_{x}$ <br> (Plane Motion) $\Sigma F_{y}=m\left(a_{G}\right)_{y}$ <br>  $\Sigma M_{G}=I_{G}$ a or $\Sigma M_{P}=\Sigma\left(\mu_{k}\right)_{P}$ |

## Principle of Work and Energy

$T_{1}+U_{1-2}=T_{2}$
Kinetic Energy

| Particle | $T=\frac{1}{2} m v^{2}$ |
| :--- | :--- |
| Rigid Body <br> (Plane Motion) | $T=\frac{1}{2} m v_{G}^{2}+\frac{1}{2} I_{G} \omega^{2}$ |

(Plane Motion)
$T=\frac{1}{2} m v_{G}^{2}+\frac{1}{2} I_{G} \omega^{2}$
Work
Variable force $\quad U_{F}=\int F \cos \theta d s$
Constant force $\quad U_{F}=\left(F_{c} \cos \theta\right) \Delta s$
Weight $\quad U_{W}=-W \Delta y$
Spring $\quad U_{s}=-\left(\frac{1}{2} k s_{2}^{2}-\frac{1}{2} k s_{1}^{2}\right)$
Couple moment $\quad U_{M}=M \Delta \theta$
Power and Efficiency
$P=\frac{d U}{d t}=\mathbf{F} \cdot \mathbf{v} \quad \epsilon=\frac{P_{\text {out }}}{P_{\text {in }}}=\frac{U_{\text {out }}}{U_{\text {in }}}$
Conservation of Energy Theorem
$T_{1}+V_{1}=T_{2}+V_{2}$
Potential Energy
$V=V_{g}+V_{e}$, where $V_{g}= \pm W y, V_{e}=+\frac{1}{2} k s^{2}$
Principle of Linear Impulse and Momentum

| Particle | $m \mathbf{v}_{1}+\Sigma \int \mathbf{F} d t=m \mathbf{v}_{2}$ |
| :--- | :---: |
| Rigid Body | $m\left(\mathbf{v}_{G}\right)_{1}+\Sigma \int \mathbf{F} d t=m\left(\mathbf{v}_{G}\right)_{2}$ |

## Conservation of Linear Momentum

$\Sigma(\text { syst. } m \mathbf{v})_{1}=\Sigma(\text { syst. } m \mathbf{v})_{2}$
Coefficient of Restitution $\quad e=\frac{\left(v_{B}\right)_{2}-\left(v_{A}\right)_{2}}{\left(v_{A}\right)_{1}-\left(v_{B}\right)_{1}}$
Principle of Angular Impulse and Momentum

| Particle | $\left(\mathbf{H}_{O}\right)_{1}+\Sigma \int \mathbf{M}_{O} d t=\left(\mathbf{H}_{O}\right)_{2}$ <br> where $H_{O}=(d)(m v)$ |
| :--- | :--- |
| Rigid Body <br> (Plane motion) | $\left(\mathbf{H}_{G}\right)_{1}+\Sigma \int \mathbf{M}_{G} d t=\left(\mathbf{H}_{G}\right)_{2}$ <br> where $H_{G}=I_{G} \omega$ <br> $\left(\mathbf{H}_{O}\right)_{1}+\Sigma \int \mathbf{M}_{O} d t=\left(\mathbf{H}_{O}\right)_{2}$ <br> where $H_{O}=I_{O} \omega$ |

[^0]
[^0]:    Conservation of Angular Momentum
    $\Sigma(\text { syst. } \mathbf{H})_{1}=\Sigma(\text { syst. } \mathbf{H})_{2}$

