



(a) A weighted hierarchical graph with 13 vertices and dimension $n = 2$. Different colours are used to distinguish clusters.

- (1) = (1, 1)
- (2) = (1, 2)
- (3) = (1, 3)
- (4) = (2, 1)
- (5) = (2, 2)
- (6) = (2, 3)
- (7) = (3, 1)
- (8) = (3, 2)
- (9) = (4, 1)
- (10) = (4, 2)
- (11) = (4, 3)
- (12) = (4, 4)
- (13) = (4, 5)

(b) Vertex ordering

0	12	0	0	0	0	0	0	0	0	0	0	0
4	0	8	2	0	0	0	0	1	0	0	0	0
7	0	0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	4	0	0	0	0	0	0	0	0
0	0	3	6	0	3	0	0	0	0	0	0	0
0	0	3	0	3	0	0	0	0	0	0	0	0
0	0	0	6	0	0	0	3	0	0	0	0	0
0	0	0	0	0	0	6	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	3	0	0
0	0	0	0	0	0	0	0	3	0	5	0	0
0	0	0	0	0	0	10	0	0	7	0	0	12
0	0	0	0	0	0	0	0	0	11	0	0	0
0	0	0	0	0	0	0	0	0	0	0	4	0

(c) Weighted block adjacency matrix corresponding to the hierarchical graph in (a).