Example: Linear wave equation with $f \neq 0, g = 0$

The pde and initial condition are given by

$$u_{tt} - u_{xx} = 0, -\infty < x < \infty, t > 0,$$

with

$$u(x,0) = \frac{1}{1+x^2}, u_t(x,0) = 0.$$

Using the method of characteristics (MOC), the solution is given by

$$u(x,t) = \frac{1}{2} \left[\frac{1}{1 + (x-t)^2} + \frac{1}{1 + (x+t)^2} \right].$$

